

3. <u>SHOW the APPKOPKIATE INEQUALITY</u>: Use algebra. It comparison series diverges then you must show >>. If it converges, you must show << . If you are unable to do so, comparison test may not work!</p>



Some common series to use for <u>comparison</u>:

- GEOMETRIC SERIES:
- P-SERIES:

NOTE: Although the comparison test requires us to check inequalities "for all n", we only need to verify that it works "for all n past a certain point". This is because the convergence of a series is unaffected by a finite number of terms so we can effectively just start our series at a later point.

**5.** Use the COMPARISON TEST to determine if the following series converge or diverge. Be sure to provide proper justification.

00 <u>4</u> n²+3n+5 A

′B •If B is made smaller, A/B gets BIGGER! . If B is made bigger, λß alife









The COMPARISON TEST uses the relationship between terms of two series. Sometimes it can be difficult (or impossible) to show that the appropriate inequality holds, in which case we CANNOT use the comparison test. But not all hope is lost, because in reality convergence or divergence of a series only depends on the long term behavior of terms as n approaches infinity.

 $\underbrace{\mathsf{Ex}}_{n=1} \cdot \underbrace{\sum_{n=1}^{\infty} \frac{4}{n^2 - 3n - 5}}_{n=1} \quad (\text{Look Back AT } \mathbb{A})$ 

## PART 2 : THE LEGNEGT COMPANYESON TEST

If the terms of two series <u>eventually behave the same</u> (or at least as a constant multiple of one another) then they must both <u>CONVERGE</u> or both <u>PIVERGE</u>. To look at the eventual behavior of the terms, we take a limit of the ratio.

-THM: [LIMIT COMPARISON TEST]

Suppose that  $\sum a_n$  and  $\sum b_n$  are series with positive terms. If

Where  $0 < C < \infty$ , then either both series CONVERGE or both **PIVERGE**.

## RECEDERS

- 1. <u>**PETERMINE a COMPARISON SERIES**</u>: same as before.
- 2. **DOES COMPARISON SERIES CONVERGE or DIVERGE?** Use known results
- 3. <u>COMPUTE the LIMIT of</u> the same is the simplify. If limit is zero or infinity then this test is inconclusive. Otherwise, we can conclude that the original series behaves the same (converge/diverge) as comparison series.

Ex3. Use the LIMIT COMPARISON TEST to determine if the following series converge or diverge.  $A \int_{n=1}^{\infty} \frac{4}{n^2 - 3n - 5}$ 

Sof:









**CUTESTIFICIAL:** How do we know if we should use the COMPARISON TEST or the LIMIT COMPARISON TEST?

- My "Go-to" is the <u>limit comparison test</u> because I feel as though it is more efficient and works in more instances. I usually start with this.
  - If you try the limit comparison test and you get a limit of 0 or infinity, then it is inconclusive. In this case, try the comparison test.
  - Ultimately, there any many examples where both will work so it comes down to a matter of preference.